

About the Course:

"*Calculus* is the most powerful weapon of thought yet devised by the wit of man." -- W. B. Smith

" Calculus is the greatest aid we have to the application of physical truth in the broadest sense of the word."

-- W. F. Osgood

Calculus is a fascinating, powerful, and challenging topic. It is the <u>mathematics of</u> <u>change</u>. While much of what we do in Mathematics is somewhat artificial, Calculus is the mathematic of <u>real life</u>. For example:

- In algebra we find the slopes of straight lines. In calculus we find the slopes of complex curves.
- In algebra we find the area of triangles and rectangles. In calculus we find the areas under curves.

- In algebra we deal with constant speeds and motion. In calculus we deal with varying speeds and motion.
- Algebra is more regular and less real. Calculus is more real and less regular.

There are three basic parts to Calculus:

- 1. Limits the tools we use to precisely describe how a function approaches a value
- 2. Derivatives the tools we use for describing how a function changes
- 3. Integrals / Antiderivatives the tools used to give the area under the curve of a function

TextBook You will be assigned a textbook for this course, and we will be reading and working from it regularly.

Teams

You have all been added to a class Team. I will be uploading and sharing material to our class Team. Please check it regularly for announcements.

Major Units/Topics:

Unit 1

Chapter 0: Review of Pre-Calculus

Lesson 1 – Introduction to Calculus

- Lesson 2 Review of Functions
- Lesson 3 Graphing Calculators
- Lesson 4 Composition
- Lesson 5 Some Common Functions
- Lesson 6 Inverse Functions
- Lesson 7 Exponential & Logarithmic Functions

Chapter 1: Limits and Rates of Change

- Lesson 1 Introduction to Limits
- Lesson 2 Properties of Limits
- Lesson 3 Limits Involving Infinity
- Lesson 4 Continuity
- Lesson 5 Applications of Limits

Unit 2

<u>Chapter 2: Derivatives</u>

Lesson 1: The Derivative

Lesson 2: Rules of Differentiation

Lesson 3: Trigonometric Derivatives and The Chain Rule

Lesson 4: Derivatives of Exponential, Log, and Inverse Trig Functions

Lesson 5: Implicit Differentiation

Chapter 3: Applications of Derivatives

Lesson 1: Analyzing Functions Part I: Curve Sketching

Lesson 2: Analyzing Functions Part II: Maximums and Minimums

Lesson 3: Applied Maximum and Minimum Problems

Lesson 4: Distance, Velocity, Acceleration and Rectilinear Motion

Lesson 5: Related Rates

Lesson 6: The Mean-Value Theorem

Unit 3

Chapter 4: Integration

Lesson 1: Area Approximation and Riemann Sums Lesson 2: Introduction to the Definite Integral Lesson 3: The Fundamental Theorem of Calculus Lesson 4: Integrals and Antiderivatives Lesson 5: Integration by Substitution Lesson 6: The Definite Integral

Unit 4

Chapter 6: Application of Integrals

- Lesson 1: Finding the Area Under and Between Curves
- Lesson 2: Volume by Discs (Slicing)
- Lesson 3: Volume by Shells
- Lesson 4: Work
- Lesson 5: Average Value of a Function and Rectilinear Motion Revisited

Chapter 7: Differential Equations

Lesson 1: Differential Equations – An Introduction

Lesson 2: Initial Value Problems, Slope Fields, and Euler's Method

Lesson 3: Linearization and Newton's Method

Lesson 4: Numerical Approximation Methods with Integrals

Chapter 8: Supplemental Topics

Lesson 1: Exploring the Graphs of f, f' Lesson 2: Relative Rates of Growth Lesson 3: Using Calculus With Data in a Table Lesson 4: Functions Defined By Integrals

Students are expected to know the following:

- functions and graphs
- limits:
 - left and right limits
 - o limits to infinity
 - o continuity
- differentiation:
 - rate of change
 - o differentiation rules
 - higher order, implicit
 - applications
- integration:
 - o approximations
 - o fundamental theorem of calculus
 - methods of integration
 - \circ applications

Big Ideas

• The concept of a limit is foundational to calculus.

- Differential calculus develops the concept of instantaneous rate of change.
- Integral calculus develops the concept of determining a product involving a continuously changing quantity over an interval.
- Derivatives and integrals are inversely related.

Equipment Needed:

a computer with internet access and headphones/speakers in addition to a graphing/scientific calculator.

Marks Breakdown:

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- Tests/Projects (30%)
 - $\circ \quad \text{Midterm and Final Exam}$
 - o Chapter Tests
- Quizzes (20%)
 - Usually have quizzes Wednesdays and Fridays
 - Homework/Participation (20%)
- Term Projects (30%)
 - $\circ \quad {\rm Two \ Presentation \ Projects}$
 - (Applications of Derivatives, Applications of Integrals)

Links

https://curriculum.gov.bc.ca/curriculum/mathematics/12/calculus https://math.libretexts.org/Bookshelves/Calculus https://sites.google.com/site/mrkerkhoven/calculus-12 http://www.wadgemath.ca/calculus-12.html